A CONJECTURE OF KOZLOV FROM THE 1998 *PROCEEDINGS OF THE AMERICAN MATHEMATICAL SOCIETY* NON-EVASIVE ORDER COMPLEXES AND GENERALIZATIONS OF NON-COMPLEMENTED LATTICES

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Abstract. Let P be a finite poset with an element s such that

(1) for all $x \in P$, either $s \vee x$ or $s \wedge x$ exists; and
(2) for all $x, y \in P$ such that $x < y$, if $s \wedge x$ does not exist but $s \wedge y$ does exist, then $(s \wedge y) \vee x$ exists.

Kozlov conjectured in the 1998 *Proceedings of the American Mathematical Society* that the order complex of P is non-evasive.

We prove this conjecture.